

Wind Field Modeling for Formation Planning in Multi-Drone Systems

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Abstract—In multi-drone systems such as drone light shows, drones move in formation while avoiding collisions. However, few existing formation planning algorithms consider the wind fields of drones during planning. Since the wind field effect is prominent when drones have to fly close to each other, we cannot ignore the effect during planning. In this paper, we extend the reservation system in autonomous intersection management for grid-based formation planning by including a new type of reservation called non-exclusive reservations specifically for handling wind fields. We train a deep learning model to predict the deviation of a drone’s trajectory when the drone enters the wind field of another drone and then use the reservation grid to prevent collision. Based on the reservation system, we develop a new formation planning algorithm that focuses on adjusting the start times of motion plans to avoid collision. Our experimental results show that trajectory prediction can help make better decisions in task assignments for minimizing makespans.

I. INTRODUCTION

In multirobot systems, robots often move in formation while avoiding collisions. A good example is drone light shows, in which a group of drones, each equipped with a light source, forms a sequence of light patterns in a night sky (see Fig. 1). The performance of a drone light show depends on how quickly the drones can change from one formation to another. There are many works on controlling a team of robots to form and maintain a formation while the robots move together (e.g., [32]). We consider the *formation planning problem* in which a planner generates formation motion plans for drones. The formation plan ensures all drones can reach their destinations while the makespan (i.e., the longest execution time of the motion plans) is minimized.

A unique challenge in multi-drone systems is that drones can generate strong wind below and around the drones, affecting other drones. Even if a drone does not crash immediately when it enters another drone’s wind field, it can be pushed away, causing the drone to deviate from its intended trajectory. Since the region affected by a drone’s wind field can be quite large, a multi-drone planning system cannot ignore the effect of wind fields during planning, especially when drones have to fly close to each other. This is essentially true when we want to achieve a high pixel density in drone light shows.

In this paper, we propose utilizing a *reservation grid* to handle wind fields during formation planning. The idea is similar to the reservation system in autonomous intersection management (AIM), which is used to coordinate autonomous



Fig. 1: A drone formation in a drone light show.²

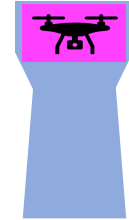


Fig. 2: Cross sections of the safety buffer (the magenta region) and the wind buffer (the light blue region).

vehicles at intersections to achieve an ultra-low traffic delay [5], [12]. In AIM, a vehicle has to reserve the set of space-time tiles on its trajectory in an intersection before it can enter the intersection. Collision avoidance can be achieved by ensuring that no two vehicles reserve the same tile. However, this reservation system is too restrictive for handling the wind fields since it is acceptable for the wind fields of two drones to overlap. Moreover, we should allow drones to enter the wind fields of other drones when it is safe to do so. Since the reservation system in AIM cannot handle wind fields properly, we propose an extension of the reservation system that allows *non-exclusive* reservations for the cells in the wind fields, such that drones can fly closer to each other and more drones can fit into the same space.

The reservation grid imposes constraints to prevent collisions and helps detect a drone entering the wind field of another drone. Instead of forbidding drones from entering any wind field, we trained a neural network model to predict drones’ trajectories under the influence of wind fields. Then, the deviated trajectories are used to make reservations in the reservation grid such that collision can be avoided. This approach allows drones to fly even closer to each other temporarily to reduce the makespan.

To illustrate the necessity of wind field modeling, we devised a new formation planning algorithm that uses goal swapping as in [32]. We show that the goal swapping rule can avoid making wrong decisions that increase the makespan if it takes the deviated trajectories into account.

In summary, the contributions of this paper are:

- We extend the reservation system for AIM with a new type of reservation called non-exclusive reservations for handling wind buffers during formation planning.
- We develop a formation planning algorithm that avoids collision by adding time delays to the start times of the predefined motion plans. To the best of our knowledge, we are the first to propose adjusting the start times of motion plans *only* to avoid collision. We state the

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²<https://pixisdrones.com/paris-hilton>

sufficient condition under which this adjustment exists.

- We trained a neural network model to predict the deviated trajectories under the influence of the wind fields of other drones. We show that trajectory prediction can improve the performance of goal swapping.

This paper is organized as follows. After presenting the related work in Sec. II, we define our formation planning problem in Sec. III. Next, we discuss what safety buffers and wind buffers in Sec. IV, and how to utilize them in the reservation grid in Sec. V. After that, we discuss how we use deep learning to model deviated trajectories in Sec. VI. Then, we describe our formation planning algorithm with goal swapping in Sec. VII. Finally, we present our experimental results in Sec. VIII and conclude this paper in Sec. IX.

II. RELATED WORK

Our multi-drone formation planning problem is a *formation reconfiguration* problem, which aims to find a formation plan that transforms an initial formation configuration into a final configuration [13]. A popular approach for formation reconfiguration is the artificial potential field (APF) method [16], [19], [28]. Zhou et al. used buffered Voronoi cells formed with locations of all peer drones to effectively intercept and box all control commands within the cells [40], an approach used by the Crazyflie platform [25]. Reciprocal n-body collision avoidance selects a safe velocity for an agent from observed peer velocities [15], [30]. Other collision avoidance approaches are chance-constrained collision avoidance for MAVs [41], bayesian policy optimization with model predictive control [4], particle swarm optimization [37], and control barrier functions [33], [36]. However, these approaches have no long-term planning for more complicated formation reconfiguration.

Some systems use decentralized approaches for formation reconfiguration. Alonso-Mora et al. presented a method based on optimal reciprocal collision avoidance (ORCA), which uses a global cost function minimization to assign target velocity and goal points to drones [3]. Bajaj and Rao presented a divide and conquer approach along with an edge following heuristic to fill the space in to display a shape while preventing oscillatory behavior and gridlock [7]. Meng et al. described gene regulatory networks with virtual DNA encoding target formation that diffuses information to other members of the swarm [20]. Wang and Rubenstein proposed a decentralized multi-agent algorithm called Walk, Stop, Count, and Swap that relies on swaps of goals between peers to resolve gridlocks [32]. They also used a local pairwise goal swap technique among the members of a swarm to reduce a cost function. Decentralized approaches typically use less computational resources and are robust against incomplete modeling of agents' behavior. However, they could be less efficient when compared with centralized approaches.

Some multiagent planning algorithms can overcome the weakness of reactive control and decentralized approaches. Yu and LaValle proposed planning optimal paths for multiple robots using integer linear programming models that optimize for makespan or distance traveled [39]. They also pro-

posed a vertex ordering structure with a scheduling algorithm for distributed distance optimal formation path planning [38]. Nar and Kotecha proposed an optimal waypoint assignment algorithm for drone light show formations.

Some works exploit local wind fields for UAV trajectory planning [22]. Lawrance et al. focused on mapping local wind fields for autonomous soaring for gliders [17]. Achermann et al. trained a neural network to predict local wind fields and used it in a sampling-based planner [1]. Chakrabarty et al. used a kinematic tree planner for time-varying complex wind fields [8]. Wirth et al. used dynamic programming for the planning process involving winds and solar radiation [34]. Chung et al. presented thermal wind field exploitation for gliders for reinforcement learning [9].

A feature of the reservation grid is the discretization of space and time. This feature is similar to occupancy grids [29], but our work is closely related to the grid-based reservation system in AIM [5], [6], [12], [26]. Wu et al. proposed a data structure called stacked reservation grid (SRG) for motion planning [35]. Lattice-based motion planners go one step further to discretize the state of robots [10], [11].

III. THE FORMATION PLANNING PROBLEM

Let \mathcal{V} be a set of n drones. A pose ρ for a drone $\nu \in \mathcal{V}$ is the position and the orientation of ν in the workspace. In a 3D workspace, ρ is $(x, y, z, \theta_x, \theta_y, \theta_z)$, where (x, y, z) is the coordinate of the center of ν and $\theta_x, \theta_y,$ and θ_z are the pitch, yaw, and roll rotations of ν . A *formation* F for \mathcal{V} is $\{\rho_1, \rho_2, \dots, \rho_n\}$, where ρ_i is a pose for $\nu_i \in \mathcal{V}$, for $1 \leq i \leq n$. A *motion plan* π for a drone ν is a sequence of control commands for controlling ν to move along a trajectory $\text{Traj}[\pi]$. A *formation plan* is $\Pi = \{\pi_i\}_{1 \leq i \leq n}$, where π_i is a motion plan for $\nu_i \in \mathcal{V}$. The execution of the motion plans in Π does not have to start at the same time. A *schedule* Γ for Π is $\{t_i\}_{1 \leq i \leq n}$, where $t_i \geq 0$ is the start time of the execution of π_i . A *timed formation plan* for \mathcal{V} is a pair (Π, Γ) . Let $|\text{Traj}[\pi]|$ be the length of the trajectory according to π , which is the time difference between the start time and the end time of the execution of π . The *makespan* of (Π, Γ) is $\text{makespan}(\Pi, \Gamma) = \max_{1 \leq i \leq n} \{t_i + |\text{Traj}[\pi_i]|\}$, which is the duration of the execution of Π given Γ .

At any time, a drone ν has a *safety buffer* and a *wind buffer* (see Fig. 2). A safety buffer is a 3D region around ν that is used to keep ν from flying too close to other drones. A wind buffer is a 3D region in the wind field generated by ν such that the wind speed at any point in the wind buffer is larger than a given threshold. The shapes of these buffers depend on the speed and the heading of a drone. We will discuss the modeling of these buffers in Sec. IV.

Given a timed formation plan (Π, Γ) , let ∂_i and ξ_i be the sequence of safety buffers and the sequence of wind buffers of $\nu_i \in \mathcal{V}$, respectively, when ν_i flies along the trajectory according to the motion plan π_i starting at time t_i . The timespans of the buffer sequences begin at time 0 and end at time $t_{\text{end}} = \text{makespan}(\Pi, \Gamma)$. We say two buffer sequences *overlap* if and only if there exists a time t at which the buffers at time t overlap. We define the *buffer profile* of ν_i

given π_i and t_i as a pair $\text{Buf}_i = (\partial_i, \xi_i)$. We say Buf_i and Buf_j are *fully compatible* if and only if 1) ∂_i and ∂_j do not overlap, 2) ∂_i and ξ_j do not overlap, and 3) ∂_j and ξ_i do not overlap. These conditions state that the safety buffer of a drone cannot overlap with the safety buffer and the wind buffer of another drone at any time. However, they allow the overlap of the wind buffers in ξ_i and ξ_j . We say Buf_i and Buf_j are *partially compatible* if and only if ∂_i and ∂_j do not overlap. In this work, it is sufficient to consider partial compatibility since we allow drones to enter the wind fields.

A timed formation plan (Π, Γ) is *valid* if and only if the buffer profiles of every pair of drones are partially compatible. We define the drone formation planning problem as follows. Given 1) a set \mathcal{V} of n drones, 2) an initial formation F_0 , and 3) a goal formation F_{goal} , find a valid timed formation plan (Π, Γ) such that $t_{\text{end}} = \text{makespan}(\Pi, \Gamma)$ is minimized while the formation at time t_{end} is F_{goal} .

IV. SAFETY BUFFERS AND WIND BUFFERS

The shapes of safety buffers and wind buffers depend on the physical characteristics, the velocity, and the heading of drones. Safety buffers should generally be large enough for emergency stops when a drone senses an imminent crash. One way to determine the minimum stopping distance is to measure the overshooting distances of a drone by conducting experiments in which we issue a stop command to a drone flying at high speed. Fig. 3 shows the overshooting distance of our drone when we issued a stop command to stop our drone flying at speed v and at angle θ relative to the horizontal plane. Thus, the minimum stopping distance is the overshooting distance. The sequence ∂_i of safety buffers can be defined using a list of cylindrical shapes, each slightly larger than the drone. More precisely, ∂_i is the union of all cylindrical shapes along a straight-line path whose length is the minimum stopping distance and whose direction is θ .

The wind buffer is defined in the same way, except that the cylindrical shape is replaced by a different shape. We used a handheld anemometer to measure the maximum wind speed at locations around and below our drone in a stationary pose. At each location, we rotated the anemometer to measure the wind speed at different angles and then identified the maximum wind speed at the location. The set of anemometer readings constitutes an estimation of the wind field around the drone. Fig. 4 shows the wind field of our drone at 1.5 m above the ground. Then, we define a shape larger than all locations with a maximum wind speed larger than a certain threshold $V_{\text{wind}}^{\text{min}}$. For simplicity, we define the shape as a union of simple geometrical shapes such as cylinders and cones. The sequence ξ_i of wind buffers is the union of the sequences of this shape along a straight-line path whose length is the minimum stopping distance and whose direction is θ . We shall assume the wind field of a drone in non-stationary poses can be larger than the wind field in stationary poses. Thus, the geometrical shapes will scale with the speed of the drone. We ignore the effect of the environment on wind fields by assuming that drones will not fly too close to walls or ground. For more information about wind field modeling,

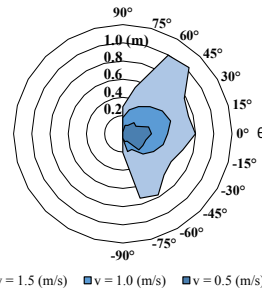


Fig. 3: The overshooting distance when our drone flies at speed v and at angle θ .

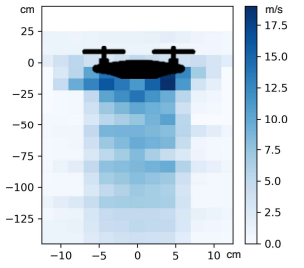


Fig. 4: A wind field of our drone at 1.5 m above the ground.

please refer to [24], which analyzes the aerodynamic effects of UAVs in the proximity of walls and ground.

V. THE RESERVATION GRID

As in AIM [5], [12], we define a *reservation grid*, which subdivides the 3D workspace into a set of equally-sized *cells*, each of which is a small region that drones can reserve. The timeline is also discretized into a sequence of equal-length *time steps*. A *tile* is a pair (c, t) , where c is a cell and t is a time step. Unlike AIM, our reservation grid has two kinds of tile reservations. In a *non-exclusive* reservation, a tile can be non-exclusively reserved by multiple drones: after a drone non-exclusively reserves a tile, other drones can still non-exclusively reserve the tile. In an *exclusive* reservation, a tile is solely reserved by one drone; after a drone exclusively reserves a tile, other drones cannot non-exclusively or exclusively reserve the tile.

We utilize the reservation grid to check the compatibility of buffer profiles quickly. Given a buffer b_t at time t , let T_{b_t} be the set of tiles whose cells overlap with b_t at t . Given a buffer profile $\text{Buf}_i = (\partial_i, \xi_i)$, the set of all tiles overlapping with ∂_i is $\text{Tile}_i^\partial = \bigcup_{b_t \in \partial_i, 0 \leq t \leq t_{\text{end}}} \{T_{b_t}\}$, whereas the set of all tiles overlapping with ξ_i is $\text{Tile}_i^\xi = \bigcup_{b_t \in \xi_i, 0 \leq t \leq t_{\text{end}}} \{T_{b_t}\}$. We call Tile_i^∂ and Tile_i^ξ the *safety buffer's footprints* and the *wind buffer's footprints* of ν_i , respectively. We can check the compatibility of two buffer profiles Buf_i and Buf_j of two drones ν_i and ν_j by 1) exclusively reserving all tiles in Tile_i^∂ and Tile_j^∂ and 2) non-exclusively reserving all tiles in Tile_i^ξ and Tile_j^ξ . If the reservations are successful, Buf_i and Buf_j are fully compatible.³ Likewise, we can check partial compatibility by exclusively reserving all tiles in Tile_i^∂ and Tile_j^∂ . Hence, we can check the validity of a timed formation plan by making reservations for the drones' footprints.

VI. MODELING THE DEVIATED TRAJECTORIES

Partial compatibility is required when a drone ν_i has to enter the wind field of another drone ν_j without collision. We would like to let one drone enter the wind field of another drone in a controlled way to reduce the makespan. To this

³Strictly speaking, Buf_i and Buf_j are *approximately* compatible since two buffers do not necessarily overlap even if they overlap with the same tile—the buffers can occupy different parts of the cell. However, these false positives are acceptable in our applications. We can avoid some of these false positives by reducing the size of the cells in the reservation grid.

end, we model how the drones' trajectories deviate from their intended trajectories under the influence of the wind field. Note that the influence is mutual—while ν_i is blown away by ν_j , ν_j could deviate from its trajectory slightly.

We trained a deep learning model to predict the trajectories of multiple agents from their past trajectories. Social LSTM [2] was first proposed to predict the future trajectories of people based on their past positions. [31] added an attention mechanism to Social LSTM, which captures the relative importance of each person when navigating in the crowd. [14] replaced LSTM with transformer networks for trajectory forecasting. [18] is a new take on the multi-modal prediction of pedestrian trajectories using transformer networks and graph convolutional networks. In our experiments, we trained a Social LSTM model with an attention mechanism described in [31]. In our experiments, the training data were generated by a simulator we developed, through real drone data should be used for more realistic modeling. The simulator can simulate drone trajectories when they fly toward each other on random trajectories under the influence of the wind fields. Although the model can only be used to predict the trajectories of a small number of drones, we use model averaging to combine the outputs of the model for many random subsets of drones. Finally, we trained a model that can take the prefixes of the trajectories of an arbitrary number of drones and generate the predicted trajectories of the drones by taking the wind field effects into account. The predicted trajectories will then be used to make exclusive reservations in the reservation grids for collision avoidance.

VII. GOAL SWAPPING IN FORMATION PLANNING

Wang and Rubenstein recently introduced a distributed shape formation algorithm that allows a swarm of robots to form a user-specified shape quickly [32]. This algorithm uses a goal selector to distribute goals among agents in a swarm for scheduling collision-free paths. Each agent uses local communication to refine the goal assignment and control its position in a distributed fashion. The algorithm is a provably correct, fully distributed shape formation algorithm that can provide collision-free and deadlock-free guarantees, requiring the use of local communication only. Inspired by this goal swapping approach, we devise a version of the algorithm for centralized control settings. We improve the goal swapping technique by incorporating wind field modeling and the reservation grid in the algorithm.

A. Scheduling of Formation Plans

Given two motion plans π_i and π_j , let $\delta_{i,j}$ be the *minimum* time such that the buffer profile Buf_i of ν_i given π_i and the start time t_i is partially compatible with the buffer profile Buf_j of ν_j given π_j and $t_j = t_i + \delta_{i,j}$, where $\delta_{i,j} \geq 0$. In other words, if we delay the execution of π_j for at least time $\delta_{i,j}$ after the start time of ν_i , the buffer profiles of both drones will be partially compatible; otherwise, they will not be partially compatible if π_j starts after π_i but before $t_i + \delta_{i,j}$. We can compute $\delta_{i,j}$ by setting $t_i = 0$ and increasing $\delta_{i,j}$ from 0 to $|\text{Traj}[\pi_i]| - 1$ until Buf_i and

Algorithm 1 Find a schedule Γ that minimizes the makespan $\text{makespan}(\Pi, \Gamma)$ for a given formation plan Π .

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1: procedure OptimizeSchedule( $\Pi$ )
2:    $\Gamma_{\min} := \emptyset$ ;  $l_{\min} := \infty$ 
3:   for  $Restart = 1$  to  $Restart_{\max}$  do
4:      $K := 1$ ;  $\rho := \langle k_i \rangle_{1 \leq i \leq n}$  is a random permutation of  $1..n$ 
5:     while  $K \leq K_{\max}$  do
6:       if  $\delta_{k_j, k_i}$  exists for all  $1 \leq i < j \leq n$  then
7:          $t_{k_1} = 0$ ;  $t_{k_j} = \max_{1 \leq i < j} \{t_{k_i} + \delta_{k_i, k_j}\}$  for  $1 < j \leq n$ 
8:          $\Gamma := \{t_{k_j}\}_{1 < j \leq n}$ ;  $l := \text{makespan}(\Pi, \Gamma)$ 
9:         if  $l < l_{\min}$  then  $\Gamma_{\min} := \Gamma$ ;  $l_{\min} := l$ ;  $K := 0$ 
10:        if  $K > 0$  then undo the last swap in Line 11 if any
11:         $K := K + 1$ ; Randomly swap two elements in  $\rho$ 
12:   return  $\Gamma_{\min}$ 

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Buf_j are partially compatible. Notice that if Buf_i and Buf_j are still incompatible when $\delta_{i,j} \geq |\text{Traj}[\pi_i]|$, it is impossible that Buf_i and Buf_j are partially compatible and $\delta_{i,j}$ does not exist. It can happen when the last pose of ν_i after executing π_i blocks ν_j from reaching its goal pose with π_j indefinitely. If both $\delta_{j,i}$ and $\delta_{i,j}$ do not exist (e.g., when ν_i and ν_j fly toward each other in a straight line), the buffer profiles of ν_i and ν_j will never be partially compatible.

The following theorem states a sufficient condition for the validity of a timed formation plan.

Theorem 1: A timed formation plan (Π, Γ) is valid if there exists an ordering $\langle \nu_{k_1}, \nu_{k_2}, \dots, \nu_{k_n} \rangle$ of drones such that for any $1 \leq i < j \leq n$, δ_{k_i, k_j} exists and $t_{k_j} \geq t_{k_i} + \delta_{k_i, k_j}$.

Proof: Since δ_{k_i, k_j} is non-negative, we have $t_{k_j} \geq t_{k_{j-1}}$ for $1 < j \leq n$. Thus, $t_{k_1} \leq t_{k_2} \leq \dots \leq t_{k_n}$, which means the motion plans will be executed in the ordering $\langle \nu_{k_1}, \nu_{k_2}, \dots, \nu_{k_n} \rangle$. Moreover, the buffer profile Buf_{k_i} of ν_{k_i} given π_{k_i} and time 0 is partially compatible with the buffer profile Buf_{k_j} of ν_{k_j} given π_{k_j} and time $(t_{k_j} - t_{k_i})$ for $1 \leq i < j \leq n$, since $t_{k_j} - t_{k_i} \geq \delta_{k_i, k_j}$. Therefore, the buffer profiles of every pair of drones are partially compatible, and (Π, Γ) is valid. ■

Theorem 1 suggests a method for finding a schedule Γ for a given formation plan Π such that (Π, Γ) is valid: find an ordering $\langle \nu_{k_1}, \nu_{k_2}, \dots, \nu_{k_n} \rangle$ such that δ_{k_j, k_i} exists for any $1 \leq i < j \leq n$. Then we can compute $\Gamma = \{t_{k_j}\}_{1 \leq j \leq n}$ where $t_{k_j} = \max_{1 \leq i < j} \{t_{k_i} + \delta_{k_i, k_j}\}$ and $t_{k_1} = 0$ such that the timed formation plan (Π, Γ) is valid.

In practice, it is easy to find an ordering that makes (Π, Γ) valid since many random permutations of drones would work. However, to find Γ that yields the *minimum* makespan for a given Π , we have to enumerate *all* possible permutations of drones such that δ_{k_j, k_i} exists and $t_{\text{end}} = \text{makespan}(\Pi, \Gamma)$ is minimum. The time complexity of this exhaustive search is exponential to n , making it impractical even when n is small. Therefore, we devise a local search algorithm to return a suboptimal solution in polynomial time. Algorithm 1 is the pseudocode of our local search algorithm. The algorithm is based on the famous min-conflict heuristic, which is highly effective in many combinatorial optimization problems [21], [27]. Initially, the algorithm randomly generates a permutation ρ of the indexes of drones

Algorithm 2 The use of goal swapping to find Π_{\min} and Γ_{\min} that minimize the makespan.

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1: procedure OptimizeMakespanByGoalSwapping
2:    $\Pi_{\min} := \emptyset; \Gamma_{\min} := \emptyset; l_{\min} := \infty; K := 1$ 
3:    $\Pi$  is the initial formation plan.
4:   while  $K \leq K_{\max}$  do
5:      $\Gamma := \text{OptimizeSchedule}(\Pi); l := \text{makespan}(\Pi, \Gamma)$ 
6:     if  $\Gamma \neq \emptyset$  and  $l < l_{\min}$  then
7:        $\Pi_{\min} := \Pi; \Gamma_{\min} := \Gamma; l_{\min} := l; K := 0$ 
8:     if  $K > 0$  then undo the last goal swap in Line 10 if any
9:     if some  $\nu_1$  and  $\nu_2$  satisfy the goal swapping rule then
10:      Swap the goals of  $\nu_1$  and  $\nu_2$  and update  $\Pi$  accordingly
11:      $K := K + 1$ 
12:   return  $(\Pi_{\min}, \Gamma_{\min})$ 

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(Line 4). Then it iteratively modifies ρ by swapping the indexes in ρ (Line 11) to see whether the minimum makespan l_{\min} can be reduced (Line 9). If l_{\min} cannot be reduced after K_{\max} swaps (Line 5), the local search reaches a local minimum, and then it uses the random restart strategy to get out of local minima (Line 3). Eventually, the algorithm returns Γ_{\min} , the schedule that gives a suboptimal makespan.

B. Minimizing Makespans by Goal Swapping

We can further reduce the makespan by utilizing the goal swapping technique in [32]. We define a *goal swapping rule*, which takes ν_1, ν_2, Π , and Γ as inputs, and check whether the makespan of the two drones (ignoring all other drones) can be reduced if they swap their goals. More precisely, let ρ_1^{init} and ρ_2^{init} be the initial poses of ν_1 and ν_2 , and let ρ_1^{goal} and ρ_2^{goal} be the current goal poses of ν_1 and ν_2 , respectively. Let π_1 and π_2 be the motion plans for ν_1 and ν_2 in Π to move from ρ_1^{init} and ρ_2^{init} to ρ_1^{goal} and ρ_2^{goal} , respectively. Let t_1 and t_2 be the start times for ν_1 and ν_2 in Γ , respectively. Suppose the goal of ν_1 changes to ρ_2^{goal} and the goal of ν_2 changes to ρ_1^{goal} . Then, we compute the new motion plans π'_1 and π'_2 and the new start times t'_1 and t'_2 such that π'_1 does not collide with π'_2 . If $\max(t'_1 + |\text{Traj}[\pi'_1]|, t'_2 + |\text{Traj}[\pi'_2]|) < \max(t_1 + |\text{Traj}[\pi_1]|, t_2 + |\text{Traj}[\pi_2]|)$, we say ν_1 and ν_2 satisfy the goal swapping rule for swapping the goals of ν_1 and ν_2 .

The goal swapping rule can make wrong decisions if it ignores the wind field effect. For example, suppose two drones fly horizontally in parallel in the opposite direction at the same start time, as shown in Fig. 5. If D_1 is slightly smaller than D_2 , the drones do not swap their goals according to the goal swapping rule. However, if the wind field of Drone A pushes Drone B downward, Drone B will fly in the blue trajectory, which is much longer than D_1 , the length of the dotted red trajectory. Then, swapping the goals can reduce the makespan of these two drones since this eliminates the wind field effect. This simple example shows that the goal swapping rule could make wrong decisions if it does not consider the deviated trajectories. In general, the same mistake occurs in more complicated scenarios since the trajectories' lengths are underestimated when the wind field effect is ignored. Therefore, it is necessary to predict the deviated trajectories when using the goal swapping rule.

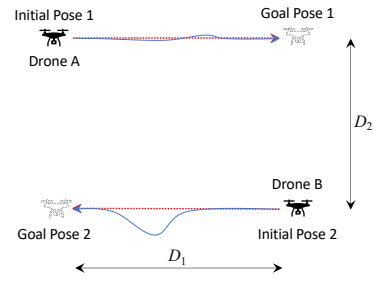


Fig. 5: A wrong decision made by the goal swapping rule.

Algorithm 2 utilizes the goal swapping rule to minimize the makespan by local search. Initially, all drones fly toward their goal poses according to the initial formation plan Π (Line 3). The algorithm randomly chooses a pair of drones that satisfies the goal swapping rule (Line 9) and then swaps their goals and updates Π accordingly (Line 10). After that, it calls *OptimizeSchedule* to find a schedule Γ for Π and compute the makespan (Line 5). If the makespan is reduced, the algorithm keeps Π and Γ as the current best solution (Line 7); otherwise, the goal swap is reverted (Line 8). The above process repeats K_{\max} times, and then the algorithm returns the best solution.

VIII. EXPERIMENTAL EVALUATION

We conducted two experiments to evaluate our algorithms. In Experiment 1, we implemented a drone swarm simulator to compare our algorithm with three baseline algorithms: 1) the intersection management (IM) approach in which drones stop and wait if another drone blocks its way [32], 2) the buffered Voronoi Cell (BVC) method [40] and 3) the artificial potential field (APF) methods [28]. In Experiment 2, we repeated Experiment 1 with a team of small-sized quadcopters called Crazyflie [25] in the real world.

Experimental Setup Experiment 1 was based on a drone simulator we developed for aerial swarm research. The simulator was implemented in C++23 with the OpenGL and SDL2 libraries. We implemented a simple drone dynamics model in which the drone can move freely in any direction subject to some speed and acceleration constraints. We retained the simulation's realism by tuning the model's parameters based on the performance of a real drone we built in our lab. The wind model was based on the wind speed measurements around the real drone using an anemometer as described in Sec. IV. The simulator can instantiate n drones and take an initial formation F_{init} and a goal formation F_{goal} as inputs. All poses in both F_{init} and F_{goal} cannot intersect with each other. The simulator controlled the simulated drones by a controller that acts according to a timed formation plan generated by our formation planning algorithm or a baseline controller such as those in the APF methods. When all drones arrive at the goal poses, the simulator will report the total execution time of the simulation as the makespan.

We implemented Algorithm 1 and Algorithm 2 as well as the three baseline algorithms in the simulator. We implemented the intersection management approach in which a drone will move toward its goal pose in a straight line,

but it will stop when a collision is imminent. A stopped drone will resume its flight when its path is clear. We implemented the buffered Voronoi Cell method based on the reference implementation in the Crazyflie system [25], which has implemented the method. We also implemented the APF method in which a drone will move according to a potential field function derived from the potential field function of its goal pose minus a weighted sum of the potential field functions of other drones. A drone will move towards its goal pose by following the gradient of the potential field.

To highlight the effect of allowing drones to enter wind fields (EWF) and goal swapping (GW), we implemented four versions of our algorithm for the four combinations of these features. To forbid drones from entering any wind fields, we replace the partial compatibility condition with the full compatibility condition when checking the validity of timed formation plans using the reservation grid described in Sec. III and Sec. V. To turn off goal swapping, we simply do not use Algorithm 2 to find the timed formation plans; instead, we use Algorithm 1 to find a schedule Γ for Π .

While our neural network is similar to the one in [31], we have to create a custom dataset of trajectories and modify a few parameters to make it suitable for inferring drone trajectories. We used a discretization of our arena of $5m \times 5m \times 3m$ motion capture space into a grid corresponding to $500 \times 500 \times 300$ volumetric data points. Position trajectories from the simulator were sampled at $0.01s$ intervals, which also served as the basis for defining a unit sequence length for the neural network. 500 trajectories with sequence lengths of $5s$ and 10 agents in constant velocity motion were generated with simulated wake interaction, which was preprocessed based on the discretization parameters and normalization. During inference, the first $0.5s$ of the straight-line trajectory sequence was used as the observed sequence, assuming that all drones began their schedule and were in motion.

In Experiment 2, we used a drone swarm system called Crazyflie 2.1 nano quadcopters to evaluate our algorithms in the real world. We used six Crazyflie drones, each of which was equipped with infrared motion tracking markers such that its position could be tracked by an Optitrack motion capture system with ten infrared cameras that offered a sub-millimeter accuracy. We ran our algorithms on a desktop computer that remotely controls the drones via a 2.4 GHz communication channel. The 168MHz ARM microcontrollers on the drones will control the drones.

Results Fig. 6 shows the results of Experiment 1. As can be seen, our algorithms always have lower average makespans when compared with the IM, BVC, and APF approaches, regardless of the number of drones. These baseline algorithms are reactive planners and do not conduct long-term planning. Hence, our planning approach clearly outperforms them in terms of minimizing the makespans.

Among the four versions of our algorithm, the version that allows drones to enter wind fields with goal swapping is the best. In fact, it is better than the other versions in two different ways. First, when compared with the versions in which drones were forbidden to enter any wind fields, the

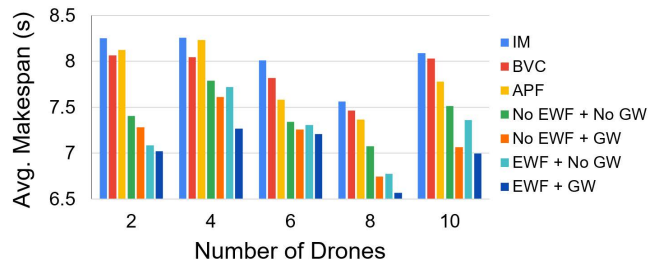


Fig. 6: Average makespan vs. the number of drones.

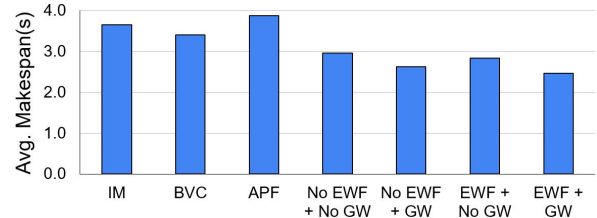


Fig. 7: The average makespans in the real drone systems.

best version outperformed them by a large margin. Clearly, it is beneficial to allow drones to enter the wind fields of other drones such that there are more ways to minimize the makespan. Second, when compared with the versions without goal swapping, the best version also outperformed them. In fact, goal swapping is better with and without the permission of entering wind fields. Therefore, goal swapping is indeed helpful in reducing the makespans. Moreover, goal swapping can yield a much larger performance improvement than allowing drones to enter wind fields.

Fig. 7 shows that the average makespans in Experiment 2 with the real drones are smaller than that in Experiment 1 due to the limited size of the room in which we conducted the experiment. Nonetheless, our algorithm outperformed the baseline algorithms in Experiment 2. Among the four versions of our algorithm, the version that allows drones to enter wind fields with goal swapping was still the best.

IX. SUMMARY AND FUTURE WORK

We have presented a new grid-based formation planning algorithm for moving a fleet of drones in formation from one location to another. Our approach utilizes a reservation grid for collision avoidance with respect to drones' safety buffers and wind fields. Wind buffers can simplify the trajectory optimization process by ignoring the irregularity of the shape of the wind fields. Our planning algorithm is a local search algorithm that aims to find a schedule of the start times of the motion plans in a formation plan with goal swapping. Our experiments with real and simulated drones show that if we allow drones to fly into the wind field of another drone, we could further reduce the makespan. One possible future work is to use reinforcement learning to find an optimal policy for formation planning with respect to wind fields in real-world applications such as interactive drone light shows [23].

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